



# Multi-way Analysis of 2D Liquid Chromatographic Metabolomics Data

Sarah E. G. Porter & Sarah C. Rutan

*Virginia Commonwealth University, Department of Chemistry*

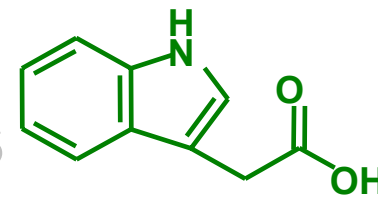
Dwight R. Stoll & Peter W. Carr

*University of Minnesota, Department of Chemistry*

Jerry D. Cohen

*University of Minnesota, Department of Horticultural Science*

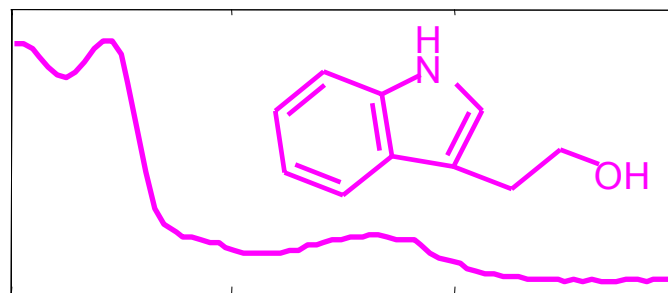
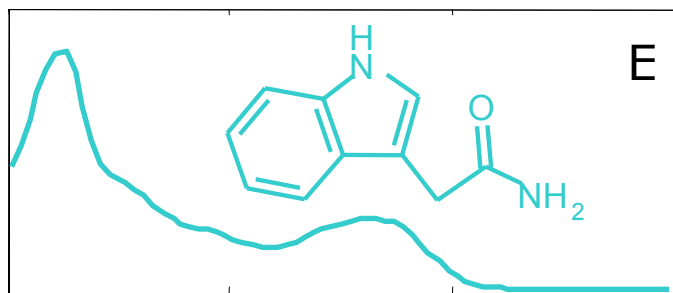
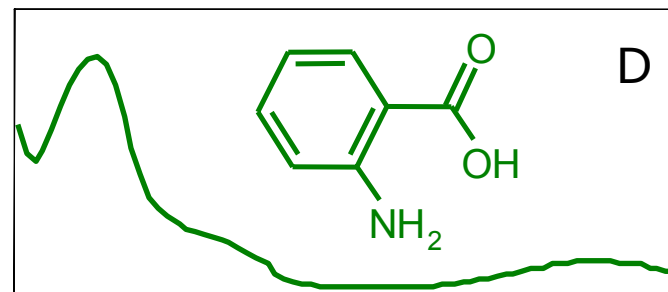
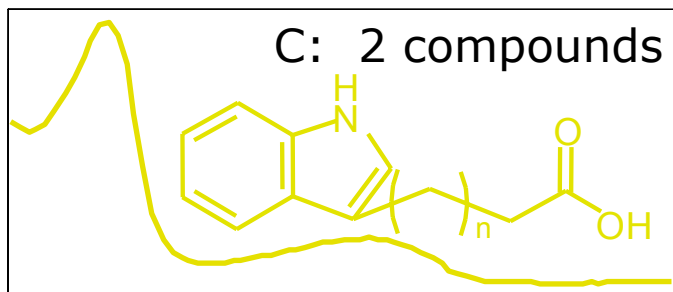
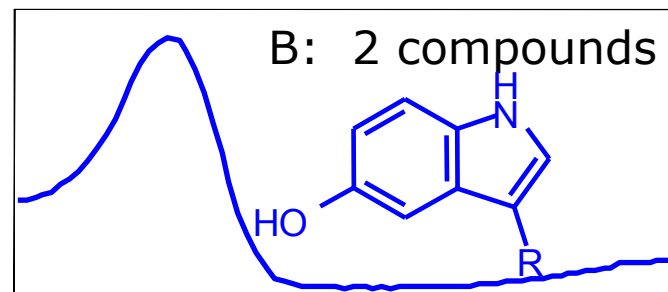
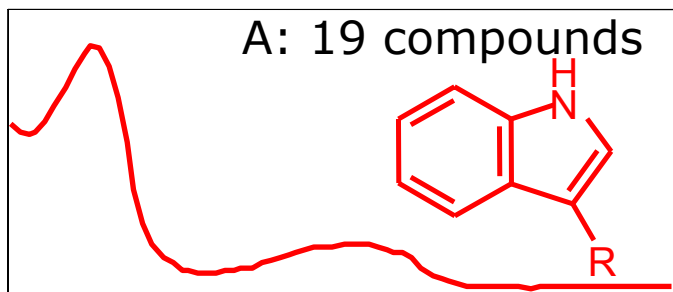
# Indole-3-Acetic Acid (IAA) in Plants



- Primary growth hormone responsible for cell division and elongation, flowering, root initiation, fruit ripening, promoting vascular tissue growth, controlling premature abscission of leaves and fruit
- Synthesized from tryptophan by a variety of pathways
- **Metabolic Profiling** – the identification and quantification of a selected group of metabolites in a biological system
- **Metabolomics** – unsupervised comparison of different biological samples to elucidate differences in metabolite levels
- **2DLC with diode array detection (DAD) was used to compare mutant and wild type maize samples to 26 indolic metabolite standards**

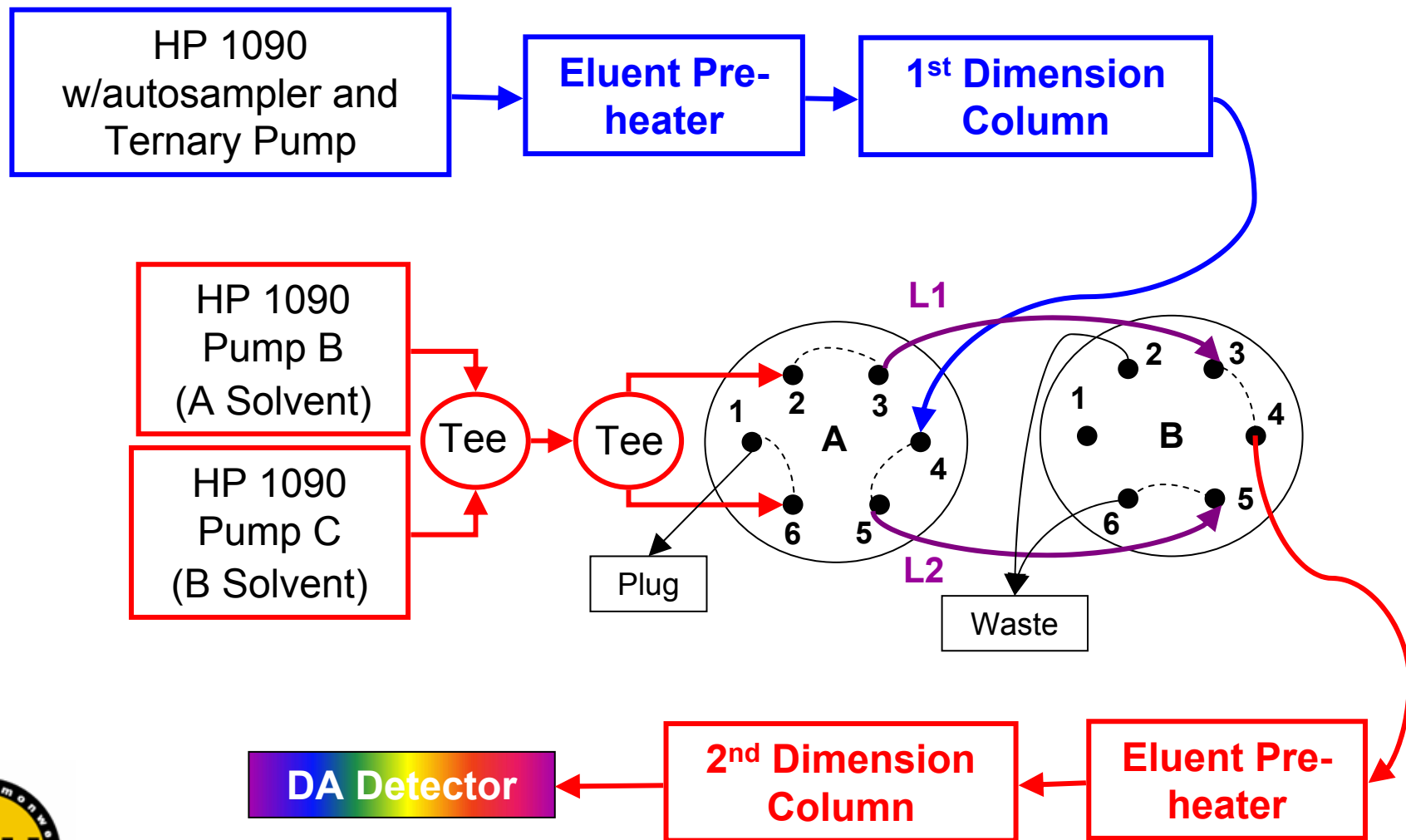


# 6 spectral components of 26 indolic standards



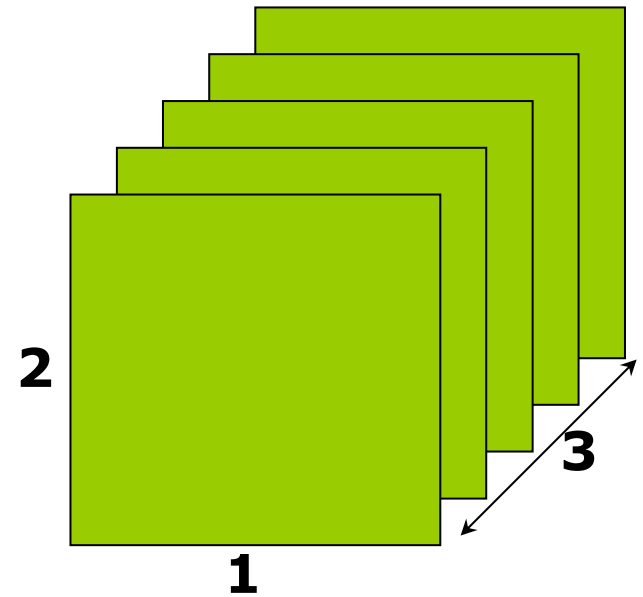
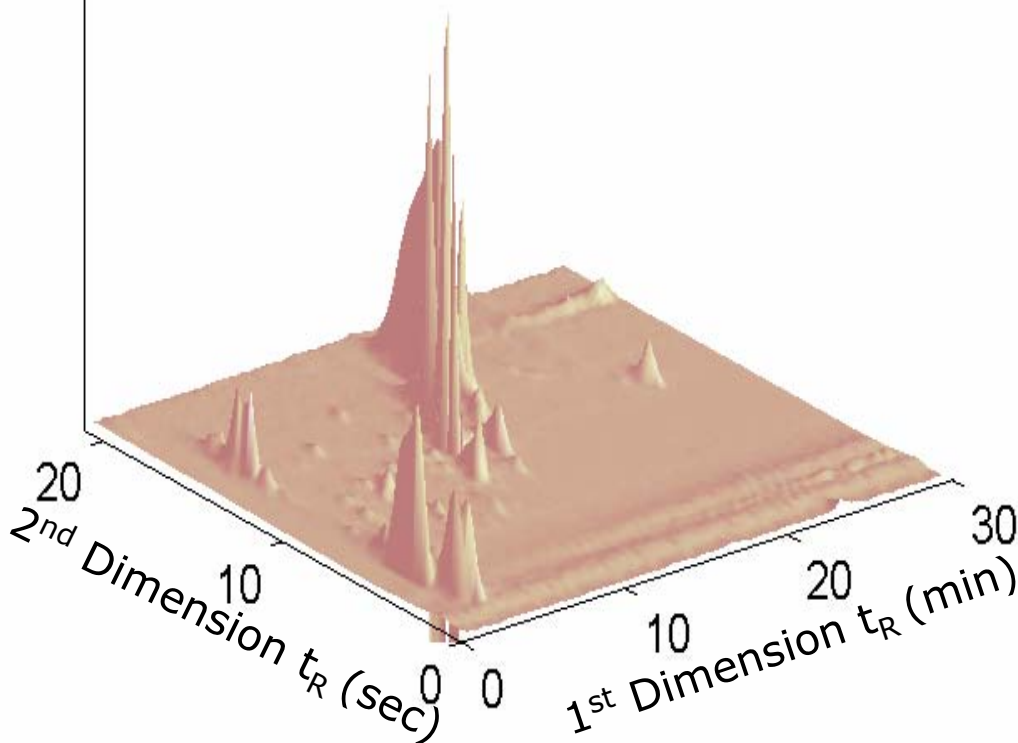
200 250 300 350 200 250 300 350  
Wavelength (nm)

# 2DLC Instrumentation Capable of Gradient Elution in Both Dimensions



# 2DLC Data Structure – Three Way Data

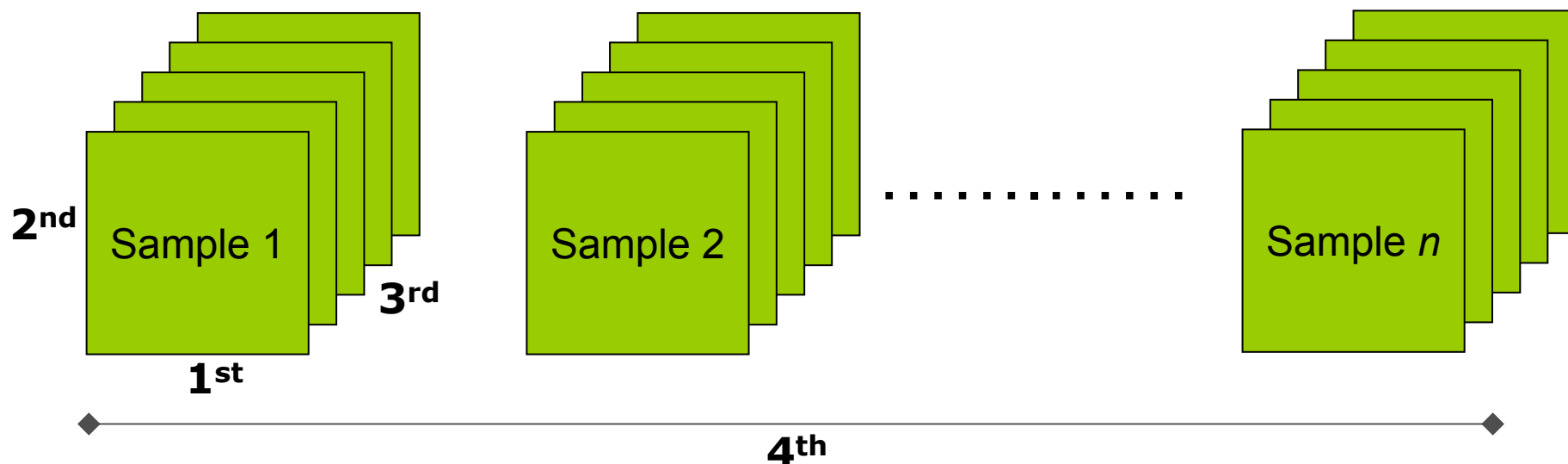
Selected Wavelength Chromatogram  
(200 nm)



Data Dimensions:

1. 1<sup>st</sup> Dimension Retention Time (min)
2. 2<sup>nd</sup> Dimension Retention Time (sec)
3. Wavelength (nm)

# Four-Way Quadrilinear Data



- 1<sup>st</sup> Dimension, Retention Time, minutes
- 2<sup>nd</sup> Dimension, Retention Time, seconds
- 3<sup>rd</sup> Dimension, Wavelength, nm
- 4<sup>th</sup> Dimension, Sample number

***The instrument response of a pure component in all domains is unique, consistent, and independent of the presence of other species***



# Description of Samples

---

- Mobile phase blank
- Standard mixture containing 26 indoles
- Duplicate wild type maize seedling samples
- Duplicate *orp* mutant maize seedling samples
  - Lacks gene for tryptophan synthase  $\beta$
  - IAA is produced via tryptophan-independent pathway



# Fixed Size Image Window – Evolving Factor Analysis<sup>a</sup>

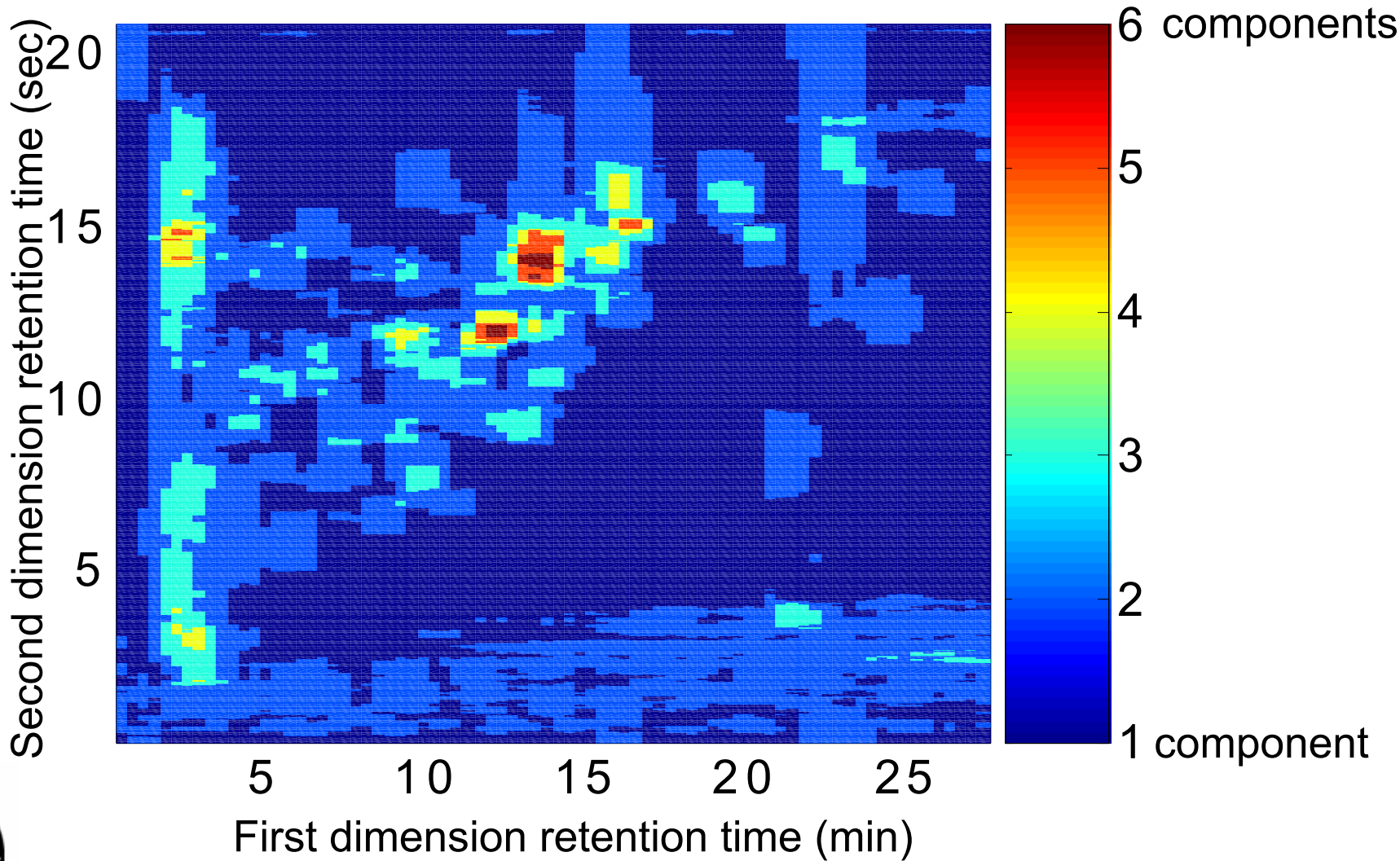
---

- FSIW-EFA uses sections of an image and performs factor analysis on a moving window
- Rank information is *local* – results estimate the complexity of an image for exploratory analysis
- Traditional EFA approaches would require unfolding of the three-way data set and loss of complex spatial structure
- **Can be used to select sections of data for subsequent analysis**

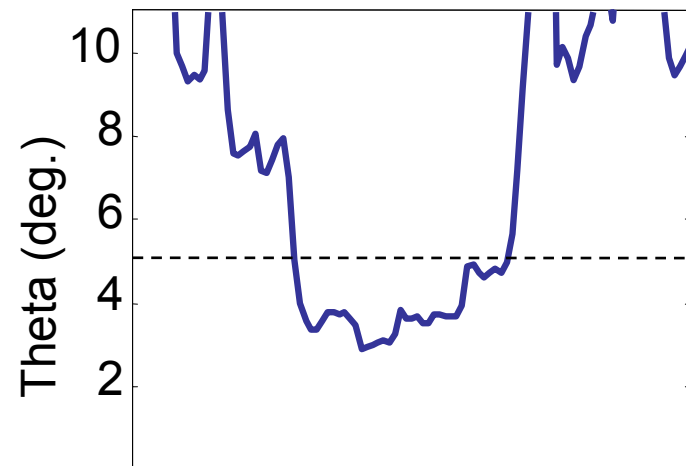
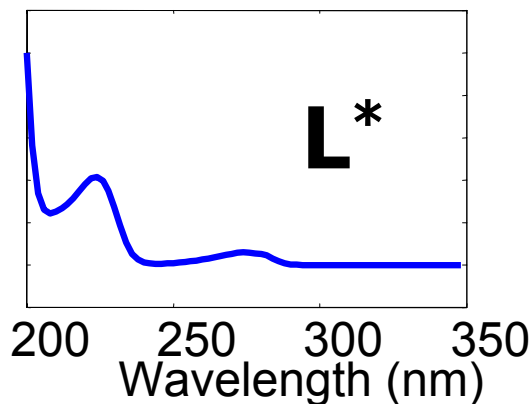
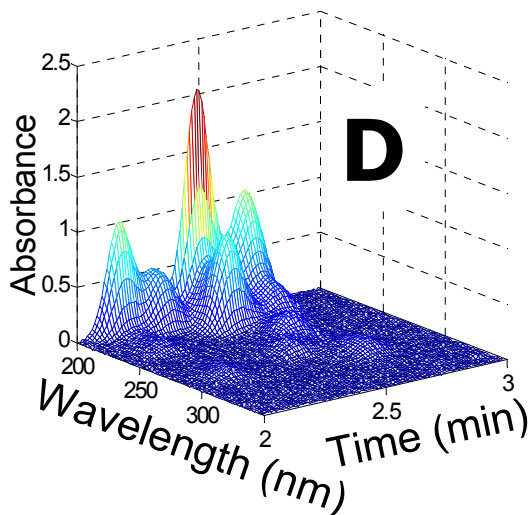




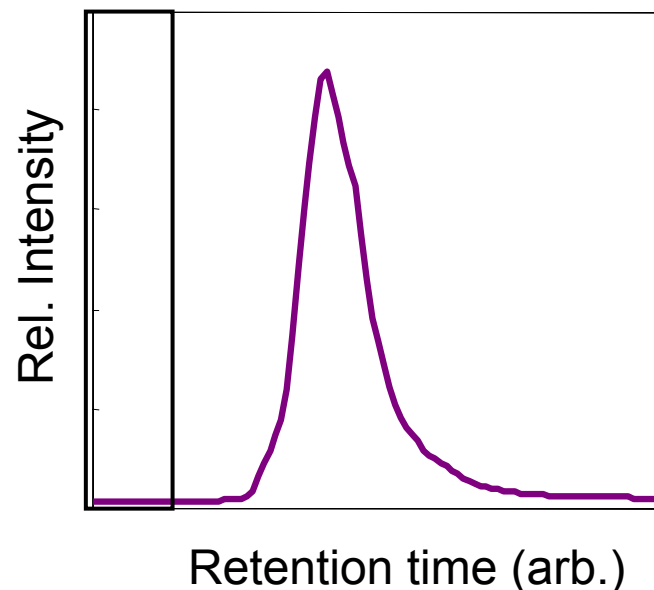
# Summed Rankmap: Standards, Wild Type, Mutant



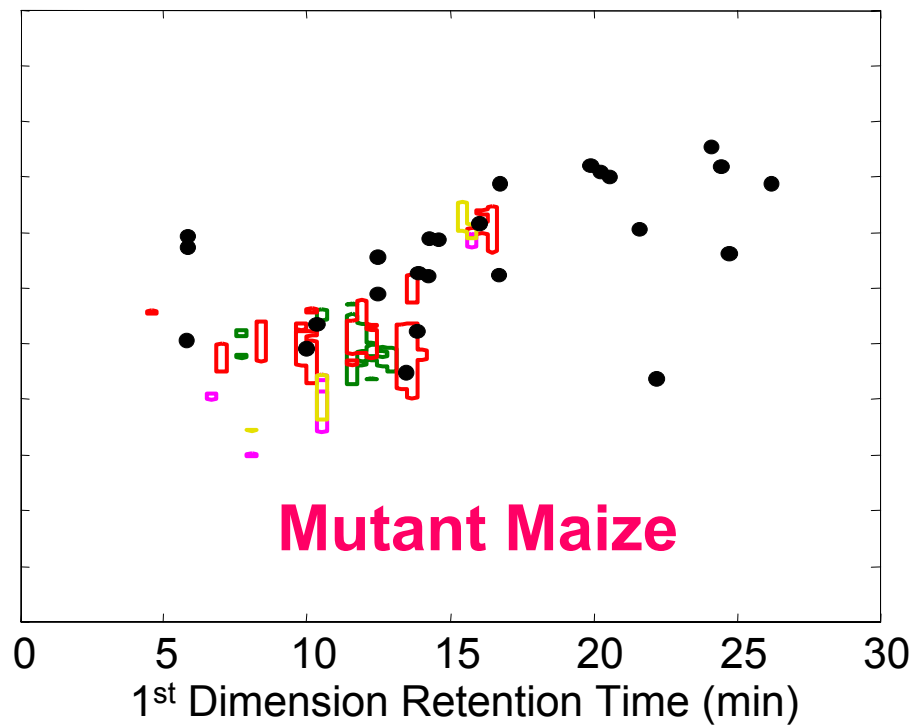
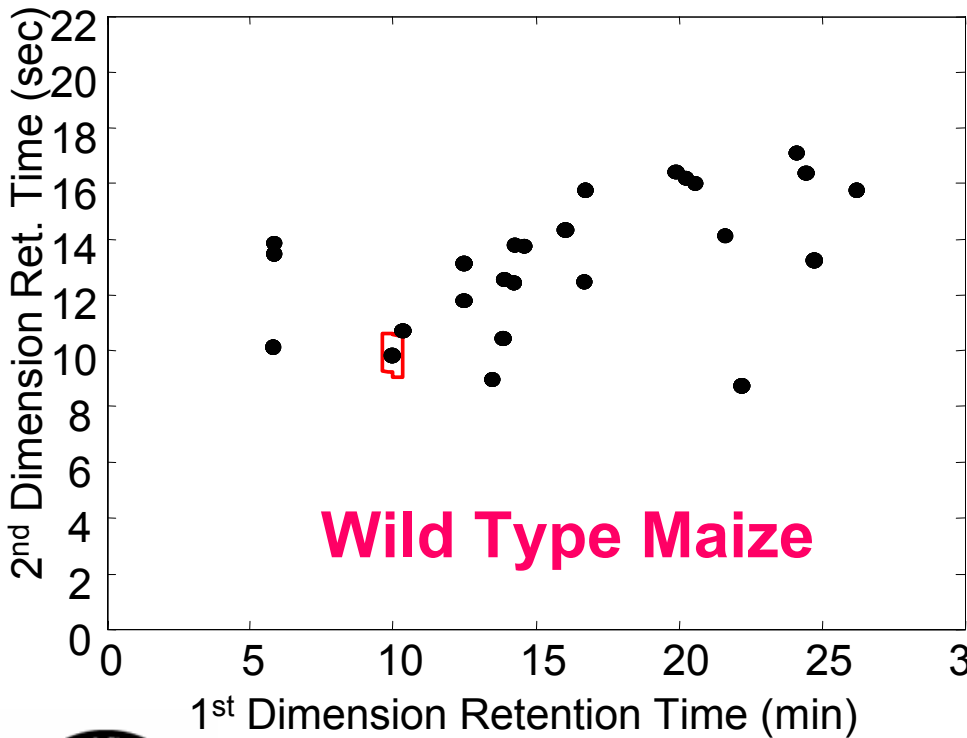
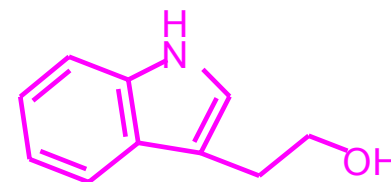
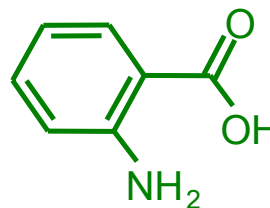
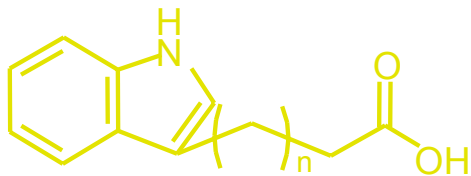
# Window Target Testing Factor Analysis



1. SVD:  $\mathbf{D} = \mathbf{U} \cdot \mathbf{S} \cdot \mathbf{V}^T$
2. Target test:  $\mathbf{T} = (\tilde{\mathbf{V}}^T \cdot \mathbf{V})^{-1} \cdot \tilde{\mathbf{V}}^T \cdot \mathbf{L}^*$
3. Rotate:  $\hat{\mathbf{L}}^* = \tilde{\mathbf{V}}^T \cdot \mathbf{T}$
4. Correlate:  $\theta = \cos^{-1} \rho$

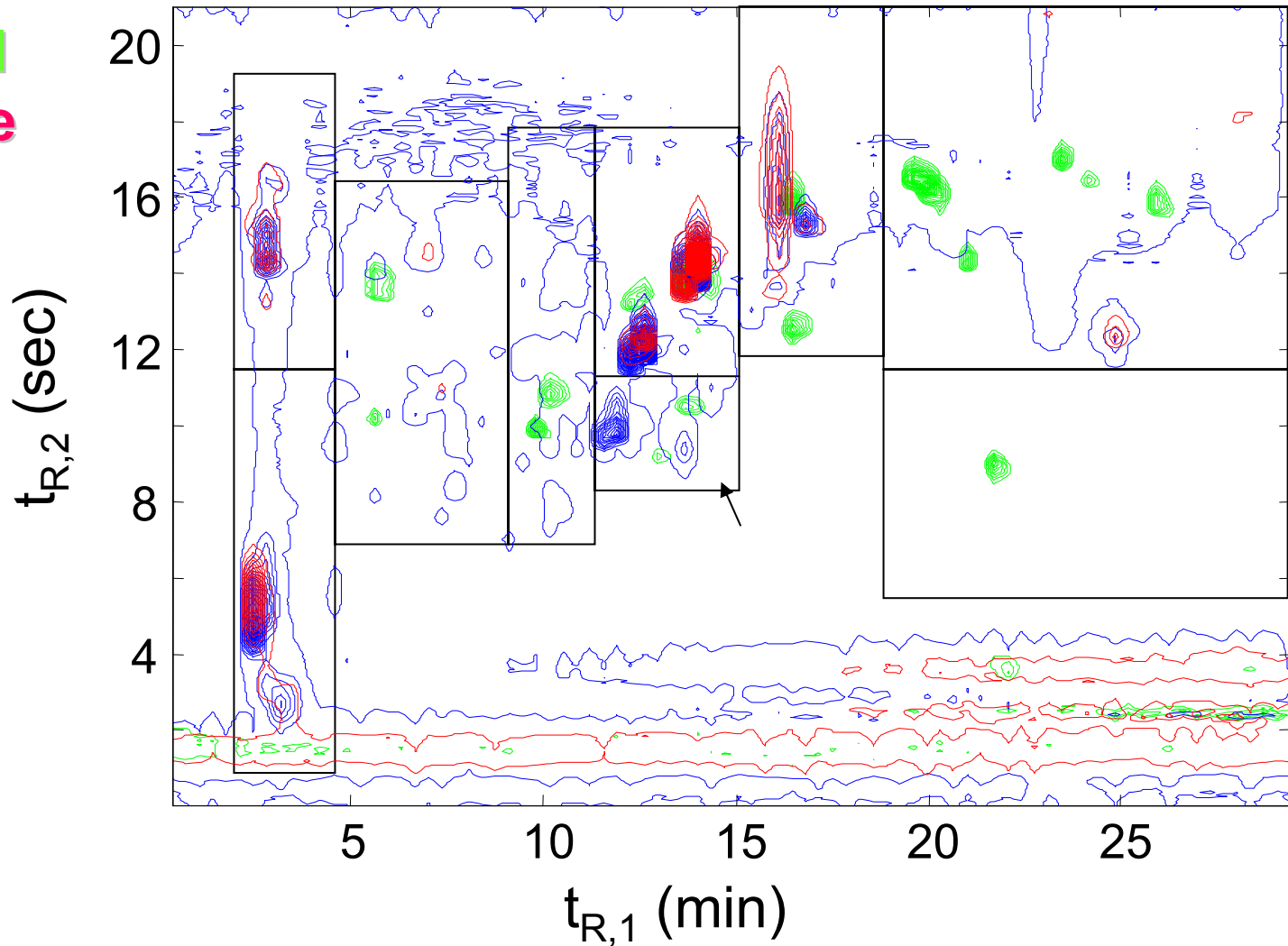


# Results of Qualitative Analysis



# 2D-Chromatograms – 220 nm

Standard  
Wild-type  
Mutant

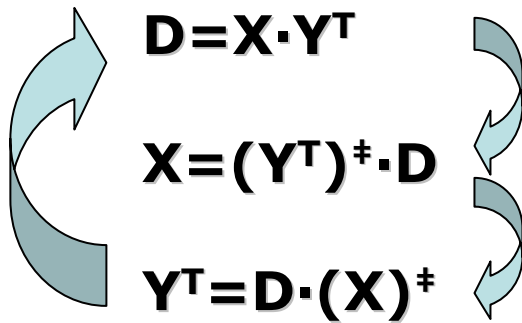


# Modeling with PARAFAC and fALS

The **four-way** PARAFAC model is represented mathematically as a sum over all of the elements of each mode (where  $c$  is the rank of the data)<sup>a</sup>:

$$d_{hijk} = \sum_{f=1}^c w_{hf} x_{if} y_{jf} z_{kf} + e_{hijk}$$

The PARAFAC model is solved using alternating least squares (ALS)



**ALS with *flexible constraints* (fALS)<sup>b</sup> allows the selective application of the unimodality constraint to selected components**

<sup>a</sup>Andersson, C. A.; Bro, R. *Chemom. Intell. Lab. Syst.* **2000**, *52*, 1-4

<sup>b</sup>Bezemer, E.; Rutan, S. C. *Chemom. Intell. Lab. Syst.* **2006**, *81*, 82-93

# PARAFAC-ALS vs. fALS

---

- PARAFAC-ALS<sup>a</sup>
  - Multilinearity required
  - Constraints provide LS solutions with guaranteed convergence
  - Constraints must be applied to all components
- fALS<sup>b</sup>
  - Multilinearity optional
  - Constraints may be ad-hoc, but not LS optimal
  - Constraints can be applied to selected components



<sup>a</sup>Andersson, C. A.; Bro, R. *Chemom. Intell. Lab. Syst.* **2000**, *52*, 1-4

<sup>b</sup>Bezemer, E.; Rutan, S. C. *Chemom. Intell. Lab. Syst.* **2006**, *81*, 82-93

# Data Analysis Procedure

---

Section data according to local complexity

Rank determination in each section

PARAFAC-ALS<sup>a</sup> – SVD initiated, non-negativity

fALS<sup>b</sup> – initiated with previous, non-negativity

*fALS<sup>b</sup> – initiated with previous, unimodality on non-background components*

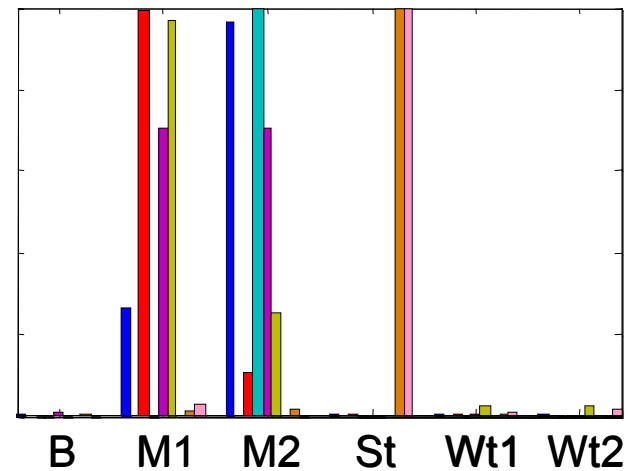
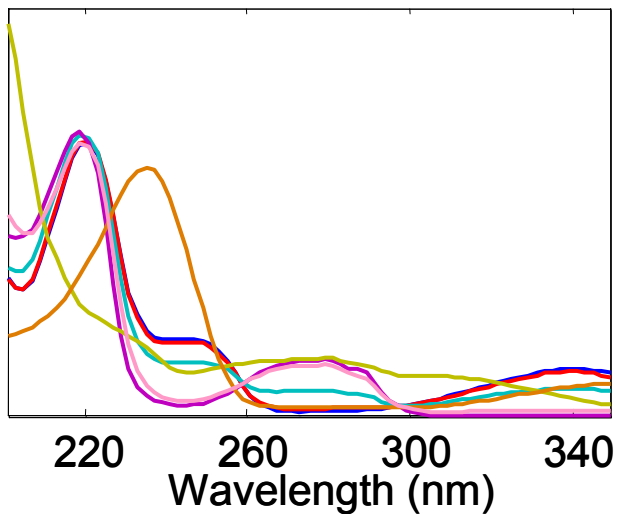
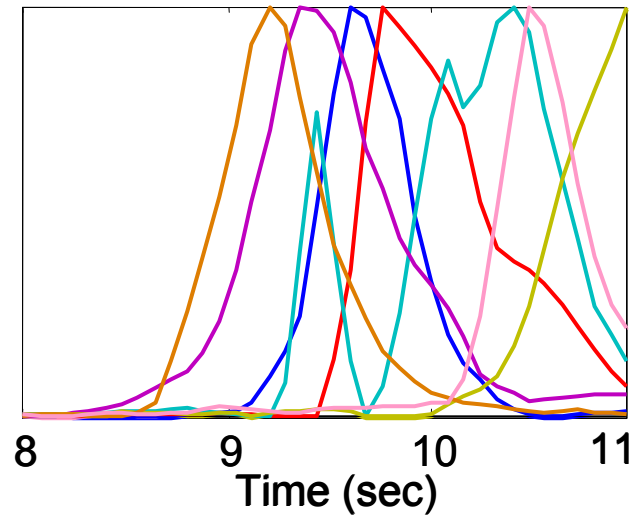
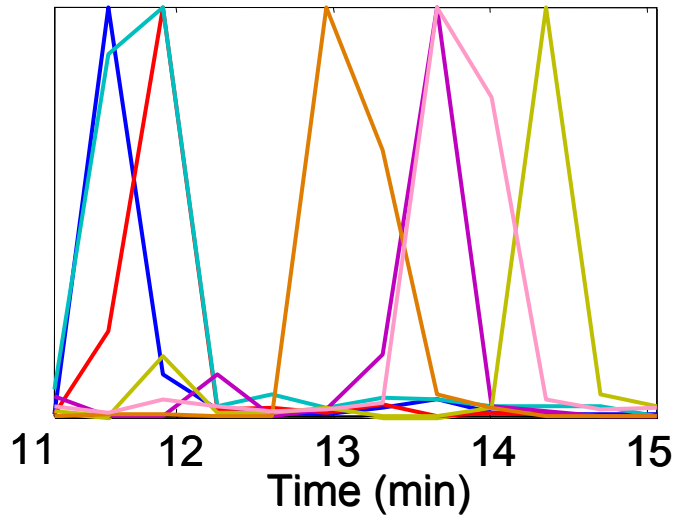
PARAFAC – ALS<sup>a</sup> – initiated with previous, non-negativity



<sup>a</sup>Andersson, C. A.; Bro, R. *Chemom. Intell. Lab. Syst.* **2000**, *52*, 1-4

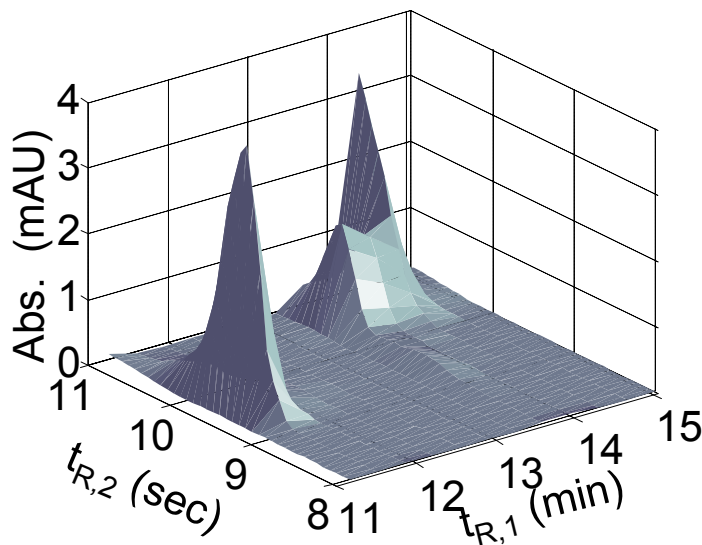
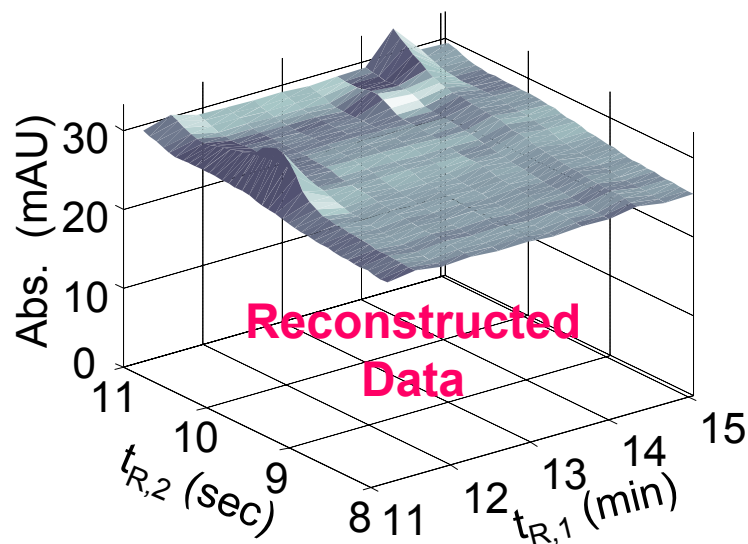
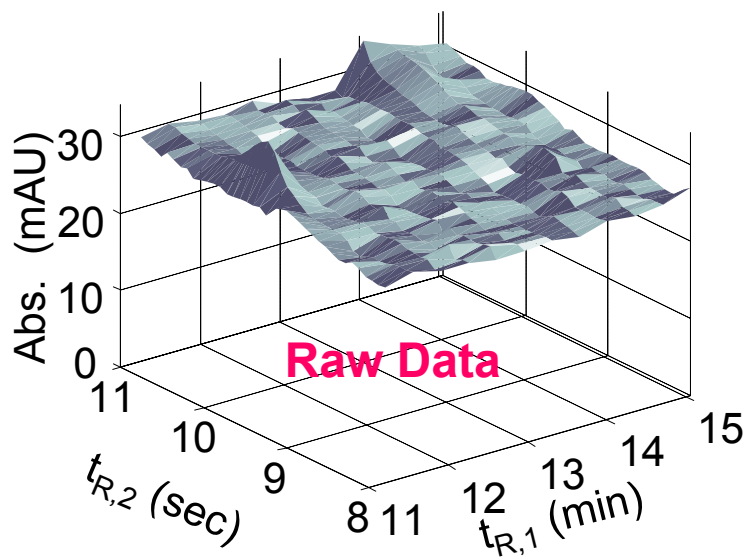
<sup>b</sup>Bezemer, E.; Rutan, S. C. *Chemom. Intell. Lab. Syst.* **2006**, *81*, 82-93

# PARAFAC Results for Selected Section



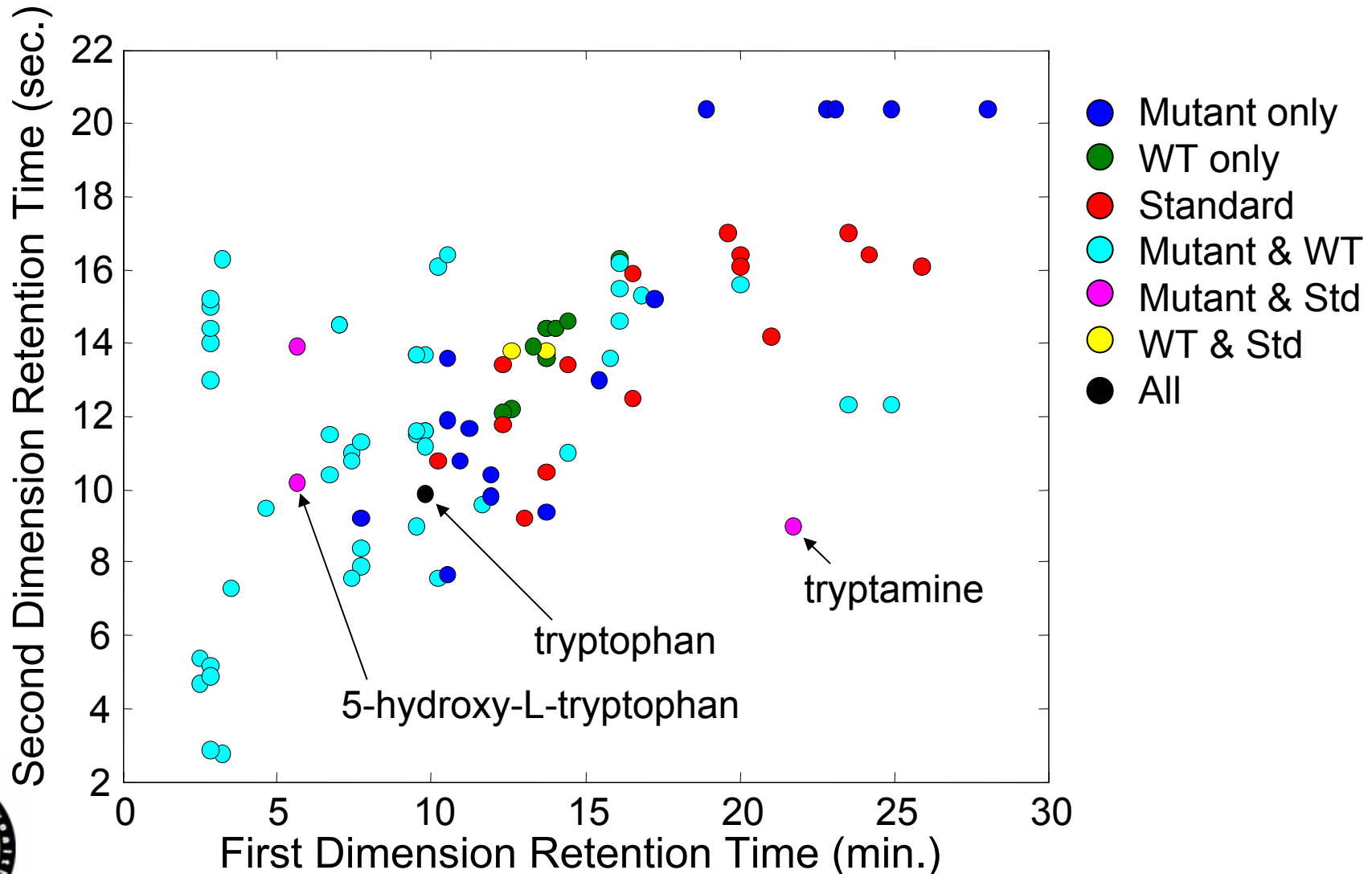


# Reconstructed PARAFAC Results – Wt1



**Reconstructed  
data with  
background  
components  
removed**

# Results of Analysis of Entire Data Set



# Quantitative Results of PARAFAC Analysis

- 95 distinct chromatographic peaks were resolved
- Many peaks showed differential expression between wild type and mutant samples

	Mutant 1	Mutant 2	WT1	WT2
5-hydroxy-L-tryptophan	ND*	0.6	ND*	ND*
Tryptophan	<b>1.4</b>	<b>1.1</b>	<b>1.8</b>	<b>1.6</b>
Indole-3-acetyl-L-alanine	ND*	ND*	0.8	0.3
Tryptamine	1.9	ND*	ND*	ND*

\*ND – not detected

Quantitative results are in  $\mu\text{g}$  of indole per gram of plant material



# Selectivity in Multi-way Analysis<sup>a</sup>

---

- Messick, Kalivas, Lang (MKL)<sup>b</sup>
  - PARAFAC
  - *Appropriate when all components are calibrated*
  - $SEL_n = \{[(X^T X) * (Y^T Y)]^{-1}\}_{nn}^{-1/2}$
  
- Ho, Christian, Davidson (HCD)<sup>c</sup>
  - GRAM
  - *Appropriate when only the target analyte is calibrated*
  - $SEL_n = \{[(X^T X)^{-1}]_{nn} [(Y^T Y)^{-1}]_{nn}\}^{-1/2}$



<sup>a</sup>Olivieri, A. C., *Anal. Chem.* **2005**, 77, 4936-3946

<sup>b</sup>Messick, N. J.; Kalivas, J. H.; Lang, P. M. *Anal. Chem.* **1996**, 68, 1572-1579

<sup>c</sup>Ho, C.-N.; Christian, G. D.; Davidson, E. R., *Anal. Chem.* **1980**, 52, 1071-1079

# Selectivity in Multi-way Analysis

---

- The selectivity calculations predict the relative decrease in precision that is observed relative to that observed for a pure sample.
- Olivieri observed that for some multi-way situations, neither selectivity formulation predicted the results of Monte Carlo calculations.
  - $SEL_{MKL}$  – upper limit of selectivity
  - $SEL_{HCD}$  – lower limit of selectivity



# Calculation of Selectivity for 2DLC vs. 2D-LC-DAD

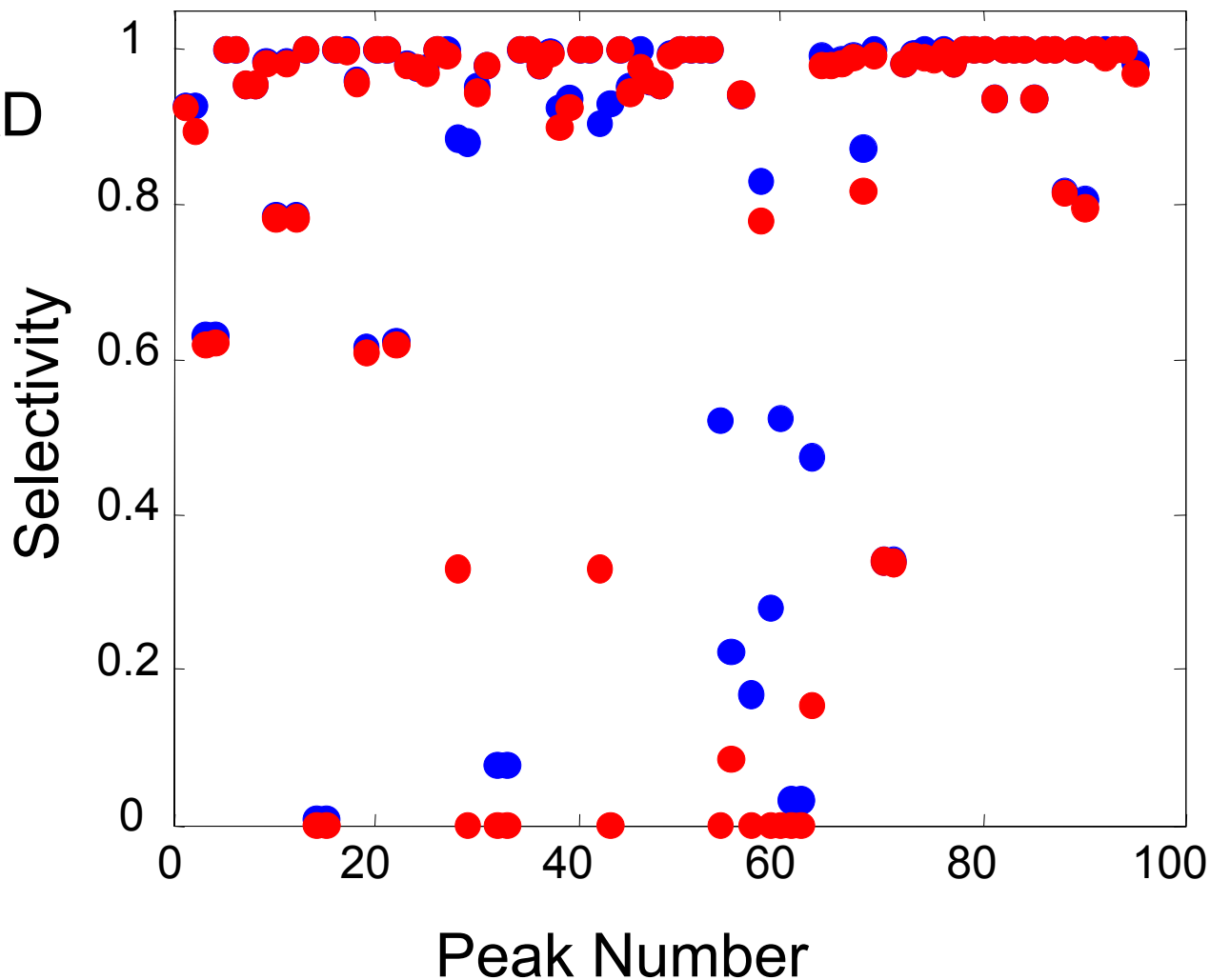
---

- **X**, **Y**, and **Z** simulated to approximate the real data
- **X** and **Y** – 1<sup>st</sup> and 2<sup>nd</sup> dimension retention profiles, using resolved retention times and simulated, Gaussian peaks
- **Z** – spectral profiles – as resolved by PARAFAC
- Background components omitted from the analysis



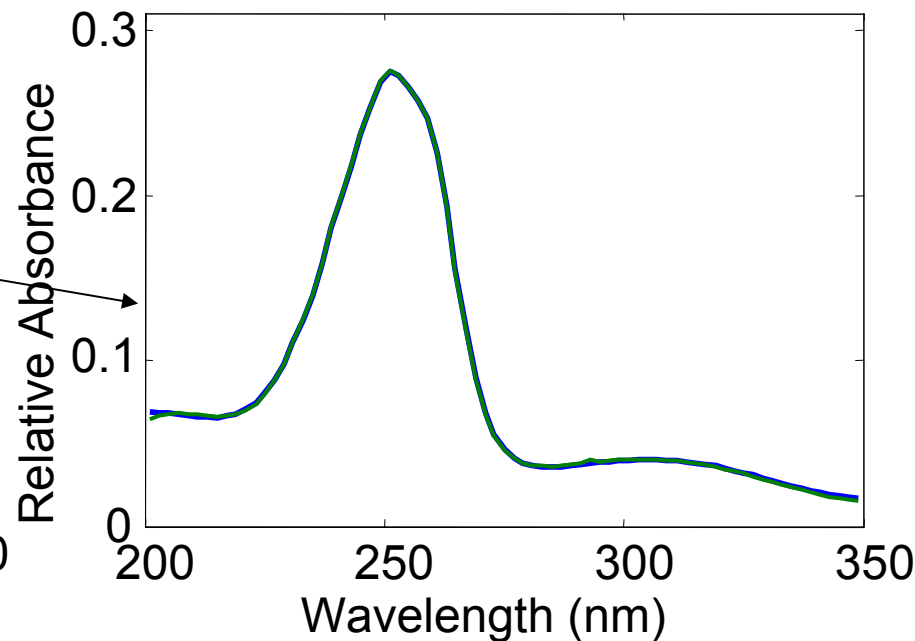
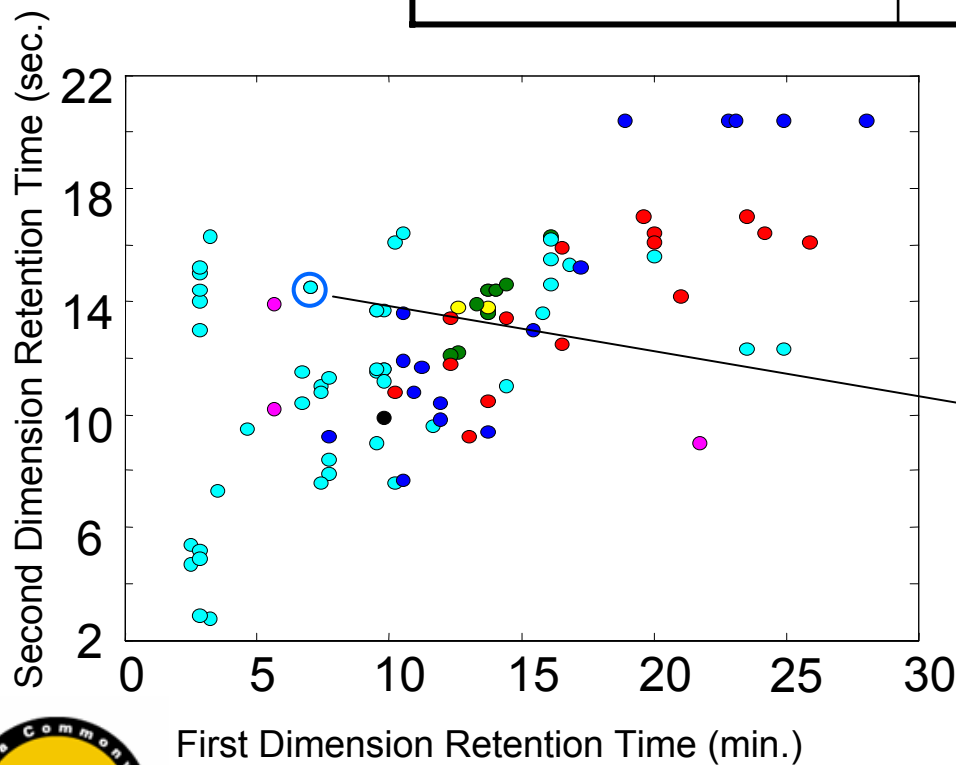
# MKL Selectivity

- 2D-LC
- 2D-LC-DAD



# MKL Selectivity – 2D-LC vs. 2D-LC-DAD

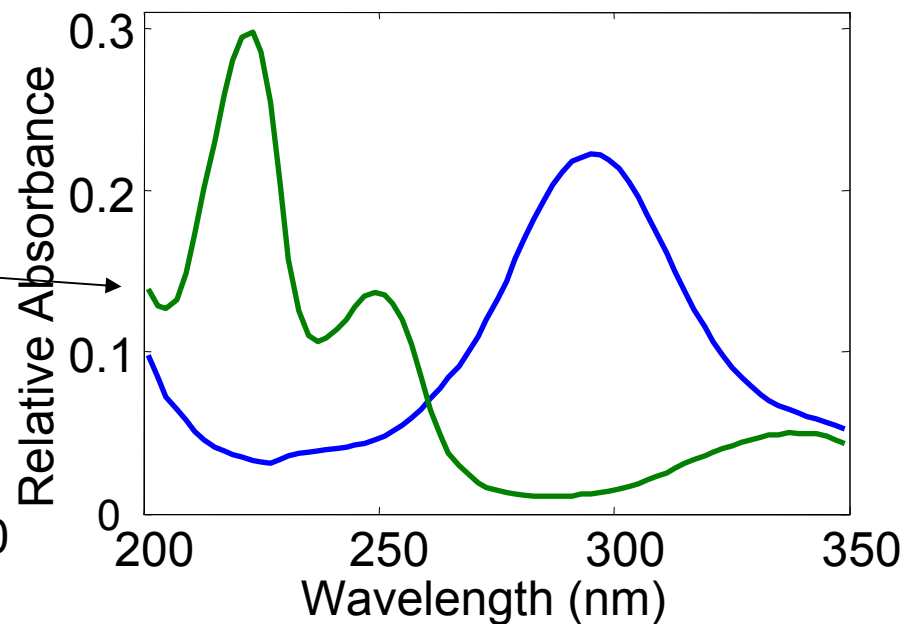
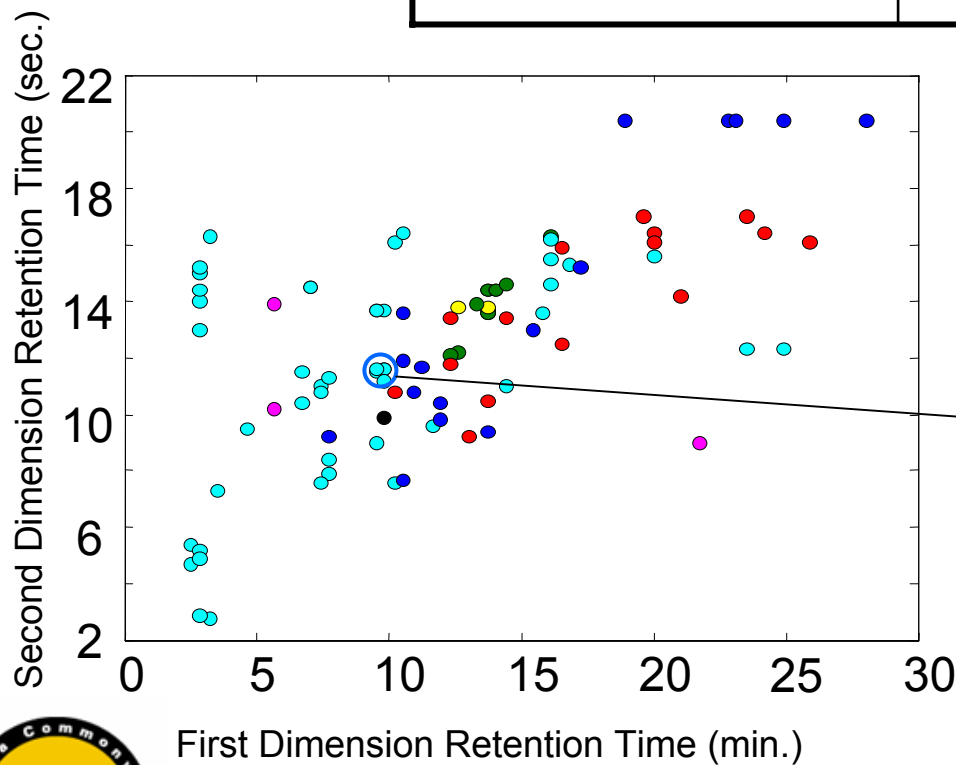
	Peak 1	Peak 2
2D-LC SEL	$1 \times 10^{-5}$	$1 \times 10^{-5}$
2D-LC-DAD SEL	$8 \times 10^{-3}$	$8 \times 10^{-3}$





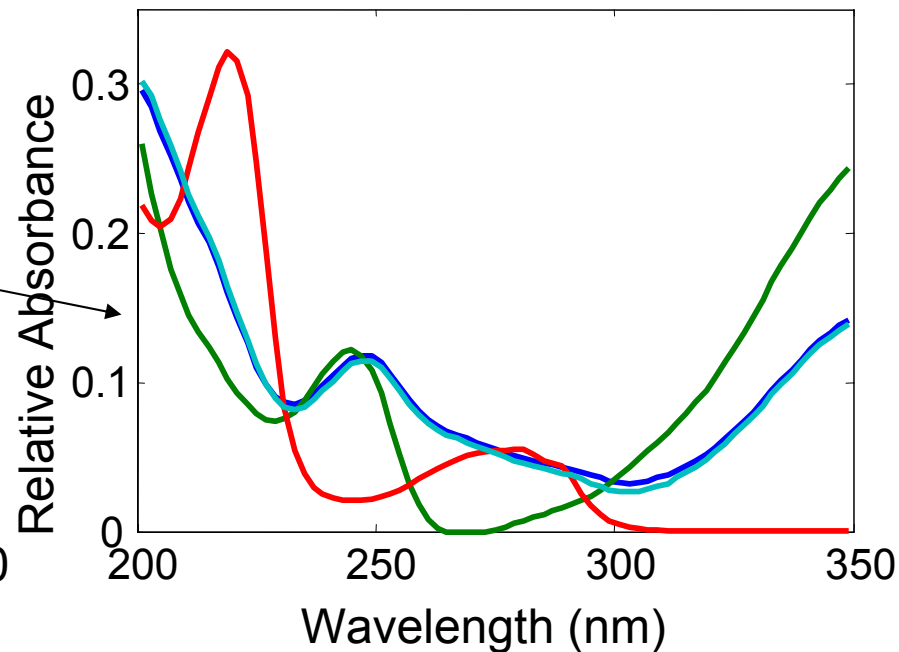
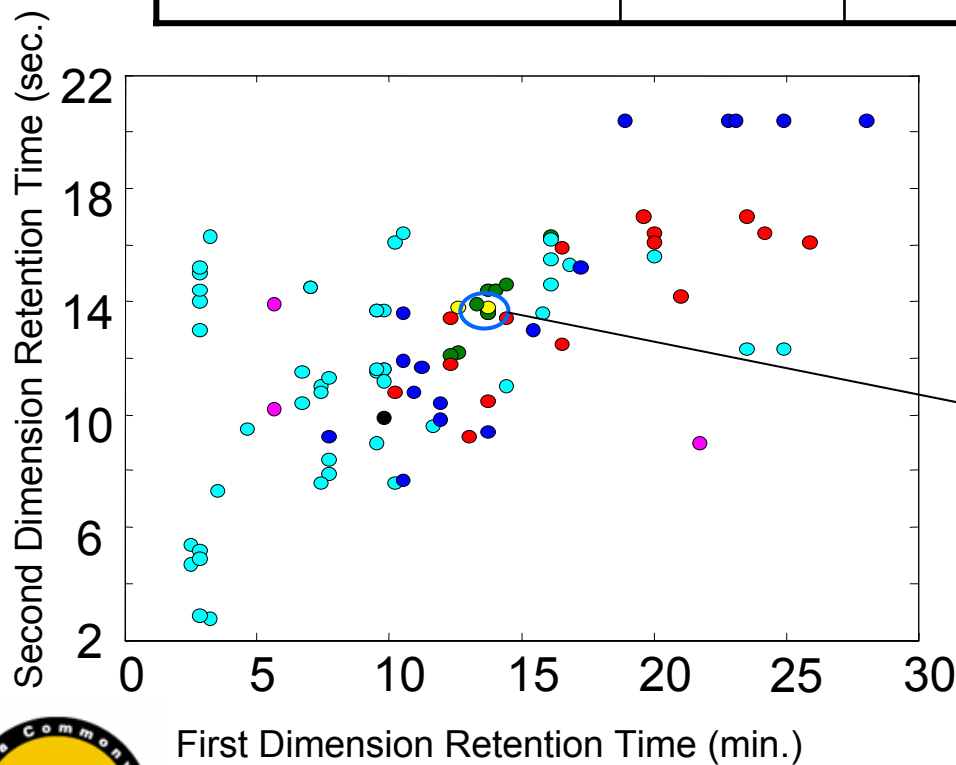
# MKL Selectivity – 2D-LC vs. 2D-LC-DAD

	Peak 1	Peak 2
2D-LC SEL	0.33	0.33
2D-LC-DAD SEL	0.89	0.91



# MKL Selectivity – 2D-LC vs. 2D-LC-DAD

	Peak 1	Peak 2	Peak 3	IAA-alanine
2D-LC SEL	0.33	0.33	0.98	0.16
2D-LC-DAD SEL	0.89	0.91	0.98	0.48



# MKL Selectivity Comparisons

---

<b>Data Dimensions</b>	<b>Average selectivity per component</b>	<b>Peak Capacity</b>
Column 1, single wavelength	0.15	50
Column 1 + DAD	0.36	n.a.
Column 2, single wavelength	0.05	17.4
Column 2 + DAD	0.25	n.a.
2D-LC, single wavelength	0.78	870
2D-LC-DAD	0.84	n.a.



# Conclusions

---

- 1. Three chemometric methods (WTTFA, PARAFAC-ALS, and fALS) have been applied to four-way quadrilinear data generated by running multiple samples with 2D-LC-DAD.**
- 2. These methods result in a great enhancement in S/N and background suppression.**
- 3. Several indole conjugates have been identified in mutant and wild type maize samples.**
- 4. The indole content of the wild type and mutants are clearly differentiated.**
- 5. The quantitative capabilities of multi-way modeling have been demonstrated.**
- 6. Multivariate selectivity has been shown to relate to chromatographic figures of merit.**



# Acknowledgements

---

Prof. Sarah Rutan's group at Virginia Commonwealth University  
Department of Chemistry

Prof. Pete Carr's group at the University of Minnesota Department  
of Chemistry

Prof. Jerry Cohen's group at the University of Minnesota  
Department of Horticulture

Ms. Vibeke Svensson, Chemometrics Group, Dept. of Food  
Science, The Royal Veterinary and Agricultural University  
(Denmark)

Supelco (Discovery HS-F5 column)

ZirChrom Separations (zirconia column)

National Institutes of Health (Grant # 5R01GM054585-09) (Carr)

National Institute of Justice (Carr)

Research Corporation (Rutan)

